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Econometric Decision Model

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ECONOMIC POLICY MAKING WITH AN ECONOMETRIC DECISION MODEL

Practical Experiences for Austria

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Abstract

This paper presents main features of a nonlinear macroeconomic model for the Austrian economy which serves as an input to derive a set of constraints for macroeconomic policy optimization. Linearized versions of the model are applied to several interactive methods for the optimization of a vector of economic policy targets using a set of mainly fiscal and monetary instruments. The techniques based on linear programming differ from each other in the information requirements and the conduct of the interaction. We consider the Step-Method (Benayoun et al. (1971)), Interactive Multiple Goal Programming (Spronk (1981)), and a method proposed by Zionts and Wallenius (1976). To assess the practical impact of methods and implementation we present results of a comparative evaluation of the techniques together with an implementation of DIDAS (developed and provided to us by the International Institute of Applied Systems Analysis, Laxenburg). People involved in practical economic policy decision making for Austria have been invited to participate. Among the participants were members of the chamber of commerce, the ministry of finance, the national bank and members of the national council. A preliminary survey of the results achieved and a critical comparative evaluation is presented.

Keywords: Interactive vector optimization; optimal economic policy making; macroeconomic model.

Contents

1 Introduction	2
2 Economic policy making with multiple objectives	2
3 Interactive optimization with multiple objectives	4
4 The econometric model	5
5 The experimental setup for interactive economic policy optimization	9
6 Conclusions	13
References	14
Appendix	17

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1 INTRODUCTION

The problem of economic policy making is to search for the joint realization of economic objectives which in most cases are in conflict with each other. There exist numerous attempts by economists to provide solutions to such problems by formulating some kind of decision models (Gruber (1983), Despontin et al. (1984), Hughes Hallett (1984)). A survey about the uses of macroeconomic models for policy formation is given by Klein (1986). By taking a normative approach of decision making the question of how to choose values for the decision variables (instruments) arises. Most approaches use an *a priori* specified preference function to derive an optimal policy. Considering the difficulty of formulating explicit preference or goal functions we intend to draw attention to the potential benefits of interactive optimization techniques for decision making with econometric models. We, therefore, shall not assume knowledge of an objective function but rather show the potential merits of an interactive procedure between the policy maker and some optimization algorithm to reach a subjectively optimal set of target values given the economic conditions in the form of an econometric model. Even for this approach one is confronted with a great number of potential techniques. We shall choose three particular ones and provide evidence with respect to their qualities when applied to a medium sized econometric model.

Most applications of multiple objective decision making (MODM) methods were intended to demonstrate the use of a particular algorithm (e.g. Despontin (1982)). Other studies that compare the performance of MODM procedures use fictitious problems which have to be solved by students, staff members of research departments or managers from industry (Wallenius (1975), Brockhoff (1985), Buchanan and Daellenbach (1987)). As far as we know, a comparative evaluation of MODM methods with a real world problem and active policy makers has not been reported.

The paper is organised as follows: Section two gives a short review of approaches to optimize economic policy with multiple objectives. The third section discusses shortly the interactive optimization techniques used and their implementation in the IAO-program package. The nonlinear econometric model with 72 equations and its properties are discussed in the fourth section. This section also discusses the problem of how to linearize the constraints relevant to policy optimization. We use the final form of the dynamic nonlinear model as a linear approximation. Section five describes the experimental design for the interactive economic policy optimization and gives a preliminary comparative evaluation. Section six concludes.

2 ECONOMIC POLICY MAKING WITH MULTIPLE OBJECTIVES

Facing real world economic policy problems, a well known approach is to simulate an econometric model for alternative policies which means to select some values for the instruments and solve for the objectives ("fixed instruments approach"). Obviously, such simulation exercises are a poor tool for finding the best policy. By considering only a small number of *a priori* specified policies, it is an inefficient method. Simulation experiments by trial and error do not exploit all information of the econometric decision model, trade-offs between objectives can not be properly examined. A consequence of the unsystematic

search process is the possible consideration of alternatives which are not Pareto optimal. Additionally, no operative framework guides the decision maker to select an optimal policy.

Tinbergen (1952, 1956) adopted the opposite view in order to reach an instrument/objective combination. He suggested to choose some values for the objectives and solve for the instruments ("fixed targets approach"). Generalizations along this line were discussed in Russel (1975), Preston (1974, 1977), and Preston and Sieper (1977).

Theil (1964) introduced explicitly an objective function supposed to represent the decision maker's preferences. He assumed that decision makers are able to express desired values for objectives and instruments. Then a quadratic cost function can be minimized under the restriction of a linear econometric model¹. Friedman (1975) analysed piecewise quadratic preference functions within this "flexible targets" approach. Further generalizations consider a dynamic objective function which leads to optimal control problems (Chow (1975), Pitchford and Turnovsky (1977), Holly et al. (1979), among others). Preston and Pagan (1982) present a unified treatment of the Tinbergen/Theil approach to the theory of economic policy. Restricted to the linear/quadratic model, the existence, uniquenesses and design of policy is analysed in a static as well as dynamic framework. Hughes Hallett and Rees (1983) give an integrated account of these methods of quantitative economic planning in which decision makers play an explicit role through descriptions of their preferences, information, and risk aversion by extending the (dynamic) optimization framework with qualitative properties.

Frisch (1961, 1976) (see also Johansen (1974)) proposed to construct an explicit preference function intended to express the preferences of the decision making authority via interviews. Basically three types of questions have to be raised to policy makers in order to identify parameters of the preference function and points of indifference. The estimation of preference parameters rather than applying interview schemes has also been considered as a tool for constructing an explicit preference function (Ancot et al. (1982), Ancot and Hughes Hallett (1983), among others).

While the explicit knowledge of a preference function is not required for conducting simulation studies, its specification is essential for the traditional optimizing framework starting with Theil's approach. Regardless of how scalar valued preference functions (or cost functions) have been constructed, a policy maker is no longer needed. Optimal policy is the outcome of a mathematical optimization exercise, a decision making process does not evolve. Such a solution to the economic policy problem may satisfy optimality conditions, but aspects concerning the quality of the decision are not taken into account. No decision process takes place. This is at variance with R. Frisch's (1976, p.92) ideas of economic policy making:

Only through such a cooperation with demonstration of alternatives will it be possible to map out to the authorities the feasible alternatives and to help them to understand which one – or which ones – amongst the feasible alternatives are the most desirable from their own viewpoint. To develop a technique of discussing feasible policy alternatives in such a scientific way is one of the most burning needs in economic policy-making today.

It turns out that interactive methods for solving multiple objective decision models are well suited for economic policy making. The next section highlights the main features of such methods.

¹Note that Tinbergen implicitly used a quadratic objective function weighting deviations from the target values infinitely high and weighting deviations from the instruments with zero.

3 INTERACTIVE OPTIMIZATION WITH MULTIPLE OBJECTIVES

Decision problems are characterized by the interaction of a decision maker, a model, and an optimization technique. Solving decision problems with multiple objectives requires methods which

- help the decision maker to clarify the complex structure of the system and confront him with trade-off choices
- pay attention to psychological and sociological aspects of decision making
- assist the decision maker to find his optimal solution
- take into account for learning effects.

Obviously, methods that first collect all preference information and then solve the problem are not the relevant ones. Decision makers often decide in a stepwise and iterative manner because they are not always able or willing to express their preferences once and for all.

By the use of interactive optimization techniques the decision process is formalized: The decision maker operates from one solution to another, guided by local preferences. Local preferences are those which are formed with respect to a current solution. The decision process is an interactive collection of preference information and iterative calculation of compromise solutions. The nature of including preference information articulated in an interaction differs between methods. The decision maker may determine or judge trade-offs among objectives, define aspiration levels (minimum or maximum values) for one or more objectives, or choose a most preferred solution from a set of (efficient) solutions.

There exists a great number of available techniques to solve multiple objective decision problems (see e.g. Hwang and Masud (1979), Despontin et al. (1983), Grauer and Wierzbicki (1984)). Here we concentrate on four interactive methods which seem to us to possess just the right qualities in order to explain the basic ideas to policy makers². We shall use the Step-Method (STEM) developed by Benayoun et al. (1971), interactive multiple goal programming (IMGP) by Spronk (1981), the method of Zionts and Wallenius (1976)(ZW) and the reference point approach as implemented in DIDAS by Rogowski, Sobczyk, and Wierzbicki (1988). As detailed descriptions of these methods are readily available in the relevant literature we shall only present the basic ideas and point out a few amendments which have been made in our computer application.

3.1 Techniques of Interactive Optimization

One can distinguish two principles of interactive techniques. One is based on the assumption of an implicitly available preference function to be optimized. However, details like weights are not explicitly known and have to be retrieved by interacting with the decision maker. The ZW-method belongs to this group. It assumes a linear preference function with unknown weights (for a concave function, see Zionts and Wallenius (1983)). By an iterative procedure which involves asking the decision maker questions concerning his preferred trade-offs between the objectives the unknown weights can be determined. The decision maker is not required to estimate his marginal rates of substitution numerically. After showing a Pareto-optimal solution, the decision maker is only requested to

²Obviously other methods also possess such qualities (e. g. Rosinger's algorithm as applied by Streuff and Gruber (1983)). Our selection was determined by easily available PC-software.

answer whether certain trade-offs presented to him are desirable, undesirable or neither. In the case of an underlying concave preference function, the decision maker additionally has to compare efficient solutions. Based on Brandner (1984), the IAO-program package derives new weights for the composite preference function from the answers in a more efficient way than suggested in the original ZW-method.

The second principle corresponds closely to the idea of satisficing. By stating bounds on the values of objectives the decision maker may change the solution space in each iteration until it shrinks to a satisfactory point. Both STEM and IMG P belong to this group of methods.

In STEM the decision maker is always confronted with a compromise solution which has been derived from the ideal (and unfeasible) solution by applying the minimax criterion. By comparing the Payoff-matrix of the initial stage with the compromise solution at each iteration, the decision maker is asked which and how much of the target values may deteriorate in order to improve at least one other objective. Using the minimax criterion as a measure of distance, the efficiency of the compromise solution is not ensured. In the IAO-program package a modified version of STEM has been implemented, so the decision maker is always confronted with an efficient solution.

In the IMG P method the decision maker has to provide his preference information on the basis of a proposed solution and a Potency-matrix which consists of a vector of ideal and a vector of pessimistic (minimum requirement) objective values. It starts from the worst possible point and enables the decision maker to indicate his wishes for improvements and to state aspiration levels. At each iteration the decision maker has to indicate whether a proposal solution is satisfactory or not and whether shifts in this solution are outweighed by shifts in a new Potency-matrix which represents a reduced objective space. A number of features already discussed in Spronk (1981) have been added to the basic IMG P algorithm and are available in the IAO-program package. Based on Müller (1985), it is possible to state aspiration levels at any iteration step. If targets are to be improved simultaneously the decision maker has the opportunity to state a weighting vector via improvement qualifications. Furthermore, an efficient solution can be presented at each iteration step.

A combination of the above mentioned two principles of interactive techniques can be found in the reference point approach as implemented in DIDAS (Rogowski, Sobczyk, Wierzbicki (1988)). The decision maker is assumed to specify aspiration levels for all objective outcomes (the reference point) in order to influence the selection of efficient decisions. A parametric scalarization of the multiobjective problem is then obtained by maximization of an order approximating achievement function where the reference point enters as parameter. As a result the user is confronted with an attainable efficient solution that is uniformly as close to the aspirations as possible. Scanning several representative efficient solutions and outcomes controlled by changing aspirations, the user should learn enough to select either an actual (subjective) decision or an efficient solution proposed by DIDAS as a basis for actual decisions. Further discussion concerning this approach can be found in Olbrisch (1988).

4 THE ECONOMETRIC MODEL

Any model is capable of representing reality only in a limited way. It is therefore obvious that also the present model cannot comply with the wishes and ideas of every possible policy maker. The optimization exercise is thus constrained by the structural information

contained in the model and its quantitative representation. We assume a constant structure of the model based on annual observations from 1964 until 1984. Recent data revisions and additions until 1987 support this assumption. The 30 stochastic equations of the model have been estimated by the ordinary least squares method where careful attention has been paid to a proper dynamic specification (Hendry (1986))³. Thus most behavioural equations exhibit an error correction mechanism. This specification approach captures both short run dynamics as well as long run information of the time series. The basic long run economic theory underlying the model specification is briefly discussed in the following.

4.1 The structural form

The macro model is basically Keynesian in spirit but contains neoclassical elements as well. Aggregate demand is the driving force of the economy, production is assumed to adjust. Disequilibrium may occur in the labour market. The fundamental building blocks of the model, which consists of 72 equations, are:

- components of real aggregate demand,
- prices and wages,
- labour market,
- formation of income,
- a small monetary sector,
- the public sector.

A main objective in model building was the explicit consideration of government economic activity with a spectrum of possible instruments. Thus, emphasis is placed on a distinction between private and public sector variables. Public consumption and investment at current prices are treated as exogenous instruments. Private sector behaviour is assumed to be governed by profit and utility maximization. Based on a CES-production technology firms derive their demand for investment goods and labour, consumers solve their consumption and time allocation problem to arrive at functions for consumer demand and supply of labour. The unemployment rate results from the interaction on the labour market. Prices are determined by the mark-up principle. Hourly wage formation is based on an expectations augmented Phillips-curve with additional working time effects. The latter are included to provide a wage compensation rule for a working time reduction policy. Price expectations are derived from the estimated consumer price equation. These expectations are not "rational" in the sense of Muth (1961). The model is not solved for them recursively. The model-generated inflation forecast affects wage increases directly in the short run. In the long run price expectations as well as changes in the legal working time do not matter.

Import and export equations depend on relative prices and an activity variable. The small monetary sector reflects the institutional fact that Austrian interest rate movements depend heavily on the international liquidity situation. The policy of pegging the Austrian shilling to the German mark suggests a close short run relationship of the respective short term rates. The movements of the long term rate are in the long run directly proportional to the short term rate and negatively proportional to real money growth (M3). The stock of the latter is explained via the multiplier mechanism of money creation transmitting the

³*PC-GIVE* (Hendry (1987)) was used to carry out the estimation. A listing of the model equations and variables can be found in the appendix C.

indirect effects of current and capital account on base money as well as required reserve and savings policy of the central bank.

In income determination the role of government as redistributor becomes obvious. Indirect taxation and subsidies finally influence the gross price level and thus the nominal value of the income to be distributed. Direct taxation of firms and households as well as the institution of social insurance determine their disposable income. The public sector budget constraint determines the changes in the stock of total public debt which in turn influences the budget via the necessary debt service. The government is assumed to control its expenditures for consumption and investment and the average rates of indirect and direct wage taxation. It also determines the level of subsidies and jointly with the "social partners" (i.e. firms and labour union representatives) the employers' share of social security contributions.

These variables, controlled by the government, will be regarded as instruments for the optimization experiments undertaken. In addition the legal working time per week (under control of the "social partners"), the rate of interest on savings deposits and the (effective) required reserve ratio (essentially controlled by the national bank) will also be considered as a policy instruments. One may also want to include the exchange rate as policy variable. However, under the current foreign exchange regime in Austria this variable can only indicate whether its changes lead to more or less favourable external conditions when compared with the current value which is basically derived from the DM/US\$ relation. It cannot be regarded as an instrument in the proper sense but may be set to some level expected by the policy maker before the optimization procedure is started.

4.2 The final form

Dynamic properties of the nonlinear model can be assessed by inspecting the final form multipliers. Starting with the last year of our sample observations 1984 a control path for the endogenous variables of the model up to 1995 is generated. For each of the aforementioned exogenous instrument variables the effects of an impulse change have been traced and are graphically displayed in figures 1 to 11. A dominant cyclical adjustment process is recognized. There seems to be evidence for stronger cycles in the adjustment of the unemployment rate. As an explanation could be offered that the dynamic specification of the labour force equation (actually an equation for the labour force participation rate) is of second order. Another feature of the dynamic profiles also catches the eye. Quite often a marked difference between the impact and the first lagged effect can be observed. This is of particular relevance for economic policy optimization as it might happen for a particular policy to have opposite effects in different periods. Thus, optimization over more than one period could prove very difficult for the decision maker and, in fact, might imply radical changes in instrument values. This fact must be borne in mind when interpreting our empirical examples. We restrict the experiment to one period only and leave the intertemporal problem for a different investigation.

A closer examination of public expenditure policy shows stronger impact of investments as compared to transfer payments on *GDP*. After about four periods their total effect is approximately the same. Investment has slight advantages when considering public debt and seems more suitable to fight unemployment than expenditures on transfers to households. Increasing the government wage bill is a relatively short run policy as far as output is concerned but stimulates inflation and increases debts in the long run. Higher subsidies cut prices at least for up to four periods and lead to higher output in turn. This

stimulation is thus responsible for the suspension of the unemployment-inflation trade off. However, with an impact multiplier above unity with respect to debts subsidies are a rather costly policy tool even in the short run.

The two types of average tax rates differ markedly with respect to their influence on prices. Raising the indirect tax rate immediately raises prices, too, but affects output only with a lag of one period. It is, therefore, better suited for a debt reduction policy than a raise in direct (wage) taxation. The latter has advantages for fighting unemployment as a fall in disposable real wages deters people from joining or staying in the labour market. The direct damping effect on real disposable wage income is more than twice as strong compared to an indirect tax rate increase. As a consequence *GDP* drops immediately by some 1.4 bill. A.S. In contrast, under higher indirect taxation *GDP* is – for the moment – slightly increased resulting from an overcompensation of the drop in private consumption by investment which is stimulated by a large fall in the real interest rate. However, the following periods bring about a much larger drop in *GDP* than under increased wage taxation so that on balance the latter is less detrimental to the growth target. Indirect taxation contributes a lot to reduce public debts but at the cost of almost all other economic objectives. Direct wage taxation avoids the push in inflation and, apart from contributing to the reduction of debts, brings about even slight advantages for the labour market.

Simulating a shortening of the legal working time seems to lend some evidence in support of such a measure to ease tensions on the labour market. It is assumed that workers receive a 0.5 % compensatory increase in their hourly wage rate for a reduction of 1 % in their working time. Up to four periods after the introduction of a one-hour-less-impulse reduction in the unemployment rate can be observed. There are also no other disadvantages to be noticed immediately. However after two periods prices pick up and output falls substantially. A long cyclical reaction takes place in the course of which inflation helps to reduce some debts. Increasing the share of employers' contributions to social security amounts to a rise in wage costs for firms. Short run effects dominate and are favourable only for government debt.

The effects of a unit change in the interest rate on savings deposits are the expected ones and relatively moderate in size. In practice, this rate plays the role of representing the financial "climate". It basically influences the long term interest rate which functions as the main monetary-real transmission mechanism via investment demand. Changing the (effective) required reserve ratio yields similar results in direction and magnitude as the interest rate change. Both could be regarded as policy substitutes for each other. A final look at the effects of a 5 % devaluation of the Austrian Shilling with respect to the US Dollar shows nothing unexpected. The familiar J-curve effect in the current account (*HDLB*) and *GDP* is accompanied by an inflation shock due to the increase in import prices and a little bit more uneasy situation on the labour market. One should bear in mind that this simulation actually represents an exercise of the effects of the DM/US\$ relation on the Austrian economy keeping the structure of the Austrian exchange rate policy fixed.

4.3 Linearization using the final form

Using linear techniques for the optimization requires the constraints to enter in linear form. One way to achieve this is to linearize the structural form of the econometric model. However, we shall not follow this approach here but we propose to use a linear approximation of the final form of the model to represent the model properties in our

optimization experiments. We assume that the dynamic multipliers are coefficients of the linearized final form

$$y_t = F(x_t, x_{t-1}, \dots, x_0; \epsilon_t, \epsilon_{t-1}, \dots, \epsilon_0)$$

with y_t a vector of endogenous variables, x_{t-k} one of the exogenous variables at period $t-k$, $k = 0, \dots, t$) and ϵ_{t-k} the vector of disturbances. Then

$$dy_t = \sum_{j=0}^t \frac{\partial F}{\partial x_{t-j}} dx_{t-j} + \sum_{j=0}^t \frac{\partial F}{\partial \epsilon_{t-j}} d\epsilon_{t-j}$$

which, approximated by finite differences, yields

$$y_t = \sum D_j x_{t-j} + \text{remainder}$$

where the remainder term includes the approximation error and lags of higher order as well as the error dynamics. For our purposes in the present paper we are going to use the simple model

$$y_t = D_0 x_t + R_t$$

where D_0 is the matrix of dynamic multipliers for lag zero. We use the values of D_0 given in *Table 1*.

TABLE 1
VALUES OF D_0 (TRANSPosed)

	<i>GDP</i>	<i>UR</i>	<i>PC</i>	<i>HDLB</i>	<i>DEFQ</i>
TRANSV	0.2597	0.0260	-0.0156	-0.3380	0.0743
OIFS	0.4595	-0.0065	-0.0140	-0.5649	0.0612
FTIV	0.2333	0.0810	1.2383	0.4189	-1.4912
NAZ	-0.1396	0.0918	-0.0269	0.0947	0.0253
FLST	-1.4312	-0.1430	0.0865	1.8631	-0.4117
EXRC	-3.2162	0.1321	2.2190	-11.6693	-0.4634
RSP	-1.7804	0.0211	0.0552	2.1895	0.0860
OPAS	0.4486	-0.0063	-0.0136	-0.5514	0.0613
SUBV	0.0077	-0.0056	-0.0928	-0.0624	0.1113
FDBSS	0.1452	0.0751	0.0877	0.0452	-0.0358
RRR	-1.6073	0.0191	0.0498	1.9768	0.0777

The planning horizon can easily be extended to cover more periods. For our practical application we have simplified the problem in order to avoid a too complicated planning issue involving intertemporal substitution effects and only consider one single period.

5 THE EXPERIMENTAL SETUP FOR INTERACTIVE ECONOMIC POLICY OPTIMIZATION

5.1 Basic data for optimizing economic policy in 1989

The following examples concentrate on achieving an optimal policy for the year 1989 given all data previous to that date. This is certainly the simplest case as it abstracts from any intertemporal considerations but should be sufficient to display relevant features of the approach. We chose as a starting point values for the objectives and instruments which are derived from the economic forecasts (March 1989) for Austria.

TABLE 2

OBJECTIVES	FORECAST	UNIT	DESCRIPTION
GDP	968.7 (3.0%)	Bill. A.S.	gross domestic product at constant prices 1976
PC	169.1 (2.8%)	Indexpoints	deflator of private consumption
UR	4.9	Percent	unemployment rate
DEFQ	3.9	Percent	net deficit as percentage of nominal GDP
HDLB	8.0	Bill. A.S.	balance of goods and services

TABLE 3

INSTRUMENTS	LOWER FORECAST	UPPER	UNIT	DESCRIPTION
TRANSV	320.0 (-4.5%)	350.0 (4.5%)	360.0 (7.5%)	Bill.A.S. gov't transfers to private households
OIFS	48.0 (-4.0%)	51.0 (2.0%)	53.0 (6.0%)	Bill.A.S. public investment at current prices
FTIV	15.0 (-5.1%)	15.8 (0%)	16.5 (4.4%)	Percent*100 average rate of indirect taxes
FLST	14.5 (-9.4%)	15.0 (-6.25%)	16.0 (0.0%)	Percent*100 average rate of direct wage tax
NAZ	38.0 (-5.0%)	40.0 (0%)	40.0 (0%)	hours/week legal working time
RSP	2.5	2.625	4.0	Percent*100 interest rate on saving deposits
EXRC	10.0	12.8	14.0	A.S./US \$ Shilling/Dollar exchange rate
OPAS	170.0 (2.4%)	174.0 (4.8%)	185.0 (11.4%)	Bill.A.S. government wage bill
SUBV	40.0 (-13.0%)	46.0 (0%)	50.0 (8.7%)	Bill.A.S. subsidies
FDBSS	0.52 (-1.9%)	0.53 (0%)	0.54 (1.9%)	Percent share of employers' contributions to social security
RRR	0.055 (-2.1%)	0.056 (0%)	0.057 (1.4%)	Percent effective required reserve ratio

For the experiments we assumed that growth of *GDP* is to be maximized, the inflation rate of *PC*, unemployment rate *UR*, and *DEFQ* are to be minimized. *HDLB* should be minimized in absolute terms (see *Table 2*). Since the growth rates of *GDP* and *PC* are chosen as targets, whereas the respective columns of D_0 in *Table 1* refer to levels, the columns are transformed appropriately.

Example runs are given in the appendix A in a form which is close to the program output.

5.2 Some evidence on a comparative evaluation of interactive methods for economic policy optimization

5.2.1 The experimental design

In contrast to earlier investigations of comparative evaluations of interactive optimization techniques we have set up a realistic problem of economic policy and not a fictitious one. We also distinguish three groups of participants in the experiment:

- One group consisted of academics and students of economics, mathematics and operations research.
- Economists and members of economic research institutions involved in advisory activity made up the second group.
- Actual economic policy makers in government and industry at the top and the advisory level formed the third group.

Together with a brief model description as above the forecast situation has been presented to the participants in the experimental evaluation. They were asked to attempt a "best" solution to the decision problem with the stated five economic objectives. A little assistance was provided to handle the software but the decisions were taken without any guidance by the operator. Each participant was presented with the same problem and only asked initially if he agreed to the proposed set of objectives and instruments, and to the bounds applied. Generally, the exchange rate was kept fix at a level of 12.5 A.S./US \$. If some participants did not agree they were free to choose their own set. The majority, however, accepted the set-up without changes.

The order in which the techniques were applied was always the same: STEM was used first, then followed IMGP and finally ZW. A part of the participants was further confronted with an implementation of DIDAS by Rogowski, Sobczyk and Wierzbicki (1988) to have an opportunity to experience a different software implementation of yet another approach to multiobjective decision support. After experiments with all methods the participants were asked to fill in a questionnaire.

We understand that an assessment of the methods is not independent of how they are implemented. The questions should, therefore, reflect both aspects which are relevant to the user but allow some discrimination as well.

The following criteria were chosen:

1. Ease of use of the method
2. Ease of understanding the logic of the method
3. Ease of providing information required by the method
4. Confidence in the final solution
5. Satisfaction with the implementation of the methods
6. Degree of learning effect
7. Potential for use of interactive MCDM techniques in concrete practical work of the participants.

Criteria 1 and 2 were assessed by ranking, 4, 5 and 6 on a point scale of 1 to 10 with higher numbers preferred to lower numbers. Criterion 3 was measured according to a scale from 1 to 6. Criteria 1, 2 and 4 are comparable to some of the criteria used by Wallenius (1975) and Buchanan and Daellenbach (1987).

5.2.2 Results

During the first half year of 1989 some fifty people in the categories mentioned above were confronted with the model and the optimization methods as described. Only 23 of them replied to the request to fill in the questionnaire. Even among those were some who did not answer all the questions. Especially many of the participants belonging to the third category of test persons felt rather uneasy about filling the questionnaire. Therefore, only four questionnaires of that latter group could be included in the sample, too few to draw significant conclusions from this batch. Most of them were strongly interested in the properties of the model and were quite indifferent concerning the optimization methods. Also, in view of the time needed to conduct one experiment, it is obvious that participants in top positions afford less time for it than do those in lower ranks. We concluded that we should stretch our experiment over a longer period in order to obtain a larger sample of the third group.

Of the remaining 19 questionnaires 11 were filled by members of the first group and 8 by those of the second one. In view of the sample size we shall not evaluate the results according to groups. We may, however, occasionally indicate if results are strikingly different across groups.

As initial information about the relevance of and the acquaintance with multiple criteria decision making among all responding participants we found that more than 80 % of the participants are facing problems with multiple criteria but only about 20 % actually use appropriate optimization techniques. Approximately 86 % of the participants think that interactive optimization techniques can sensibly be applied to their multicriteria problems.

TABLE 4

CRITERIONS 1 & 2 — AVERAGE RANKS

	STEM	IMGP	ZW	DIDAS
Criterion 1: Ease of use	1.8	2.4	3.0	2.2
Criterion 2: Understanding the logic	1.7	2.0	2.5	3.2

Ranking the four methods under scrutiny produced *Table 4*. It contains the average of the ranks achieved. STEM and DIDAS are the easiest to use – probably the implementation in IAC-DIDAS-L is partially responsible for this good result – but participants had problems to understand the logic of the reference point method. It turned out that most of the participants did not see how their result varied with variations in the reference point. In contrast the guiding principle of STEM was the easiest to understand and also easy to use. The term "ease of use" was often misunderstood by the participants as "user friendly implementation".

Providing the required information (criterion 3) was generally found relatively easy, sometimes with some need to think. Most participants did not find much difference across methods but for STEM and IMGP answering deemed a little easier than for the other two methods.

Considering aspects of the implementation *Table 5* gives point averages from a scale of 1 to 10 (higher figures preferred to lower figures):

TABLE 5
CRITERION 5 — AVERAGE POINTS

	STEM	IMGP	ZW	DIDAS
understanding interaction	7.8	6.6	6.6	6.4
clarity of information	6.7	6.5	5.5	7.5
speed	7.9	7.6	6.7	8.3
flexibility	6.5	7.3	5.0	6.3
sum	29.0	28.1	23.9	28.4

Concerning the sum of points all methods except ZW seem to do equally well. This may be due to the fact that we present the tradeoffs in terms of a tradeoff vector and not in terms of adjacent efficient solutions. The marginal (but not significant) dominance of STEM might be explained by the fact that the participant is confronted with this method first.

Turning finally to criteria 4 and 6, the degree of confidence in the solution and the degree of learning experienced, we find a higher point average for the learning effect (7.7) than for the degree of confidence (5.9). Both criteria are measured on a scale of 1 (no confidence or nothing learned from the experiment) to 10 points. It is interesting to note that academic participants varied much more in their answers than did participants of the other groups. This does not seem surprising because the number of available methods itself and the varying results associated with them makes participants suspicious about the relevance of the achieved results. In most cases, however, heated debates started about the econometric model, its properties and the consequences traced in the optimization experiments. Learning about the problem at issue was then straightforward.

6 CONCLUSIONS

This paper has presented some main features of a macroeconomic model for the Austrian economy which serves as an input to derive a set of constraints for macroeconomic policy optimization. The model does not only provide a well structured representation of the Austrian economy but also a useful and practical linkage between objectives and instruments.

Utilizing all advantages of an optimization framework for actual decision making but without the requirement of a preference function, interactive methods for solving multiple objective decision models are well suited for economic policy making. The policy maker is closely involved in the solution process. Consequently, decision quality is considerably improved because interactive optimization methods allow to pay attention to psychological and sociological aspects of decision making. Important learning effects may be induced.

Three of these optimization techniques based on linear programming are implemented in the InterActive Optimization program package IAO (Brandner and Böhm (1989)). Together with a PC-version of DIDAS they are applied to the econometric model of Austria in the context of an experiment in economic policy optimization. Example runs on economic policy optimization for a single period presented in the appendix A permit quick comparisons between the methods which differ from each other in the information requirements and the conduct of the interaction. The example runs clearly demonstrate how decision makers gain insight into the restrictions of their problem implied by the model structure and the trade-off choices to find an optimal solution. An evaluation of questionnaires

returned by the participants in the experiments permitted to draw comparisons between the methods. It is certainly not easily possible to convey in written form the process of learning – experienced by the decision maker and the model builder too – associated with real life-use of an interactive software. Therefore, the second purpose of the experiment was to assess the practical usefulness of interactive procedures for people involved in actual economic policy decision making in Austria. A survey of the results achieved so far and a critical comparative evaluation has been presented. There is clear evidence for a demand for easily accessible techniques to solve multicriteria decision problems.

There remain a number of problems most of which are too complex to be considered here, e.g. group decisions, model specification problems. Two problems seem to be immediately relevant. First, applying a nonlinear model requires certain approximations which are not always satisfactory. Nonlinear optimization techniques will doubtlessly help provided the model possesses the appropriate curvature properties. Earlier experiments of the authors indicated that this is quite often not the case (cf. Brandner 1985). Second, a dynamic model demands intertemporal considerations in decision making. Even in simple cases this amounts to a multiple of one-period-target-vectors with the consequence of a very large number of targets and correspondingly a larger number of tradeoff possibilities. Aspects of this question have been investigated already (e.g. Deissenberg (1983)) and shall be pursued with the present model-setup at a different place.

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APPENDIX A

A1.1 Interactive Economic Policy Optimization using STEM

```

*** S T E M ***
Optimize Problem   -> P
Print Objectives  -> O
Print Instruments -> I
E N D              -> *
->p

```

At this stage it is assumed that the model equations, a selection of objectives and instruments as well as bounds for the latter are already in memory.

The optimization menu has been chosen. The other entries may be used to inform the decision maker about the current values of objectives and instruments.

```

** O P T I M I Z E **
PayOff Matrix     -> P
Compromise        -> C
E N D             -> *
->p

```

To get an overview of the possible range of objective values that can be achieved. Each line of the matrix represents a single target optimization.

	PAY-OFF MATRIX				
	gdp-%	ur	pc-%	L.Bil.	defq
max: gdp-%	4.1161	5.2901	2.7513	4.8491	4.9529
min: ur	2.7463	3.9126	2.0840	10.8362	3.6009
min: pc-%	4.0490	5.3507	1.5927	5.2890	7.2410
min: L.Bil.	3.6171	4.9438	1.7413	0.0000	6.0784
min: defq	1.8158	4.2186	3.9411	23.1849	-0.9752

```

** O P T I M I Z E **
PayOff Matrix     -> P
Compromise        -> C
E N D             -> *
->c

```

Now a compromise solution is asked for.

Taking the compromise-solution:

Objective 1	gdp-%	3.50295
Objective 2	ur	4.77670
Objective 3	pc-%	3.52382
Objective 4	L.Bil.	3.18328
Objective 5	defq	2.20812

Would you accept a deterioration of one of the objectives in order to improve at least one other y / n ... y

Objective 1	gdp-%	is allowed to deteriorate about	...	*
Objective 2	ur	is allowed to deteriorate about	...	*
Objective 3	pc-%	is allowed to deteriorate about	...	*
Objective 4	L.Bil.	is allowed to deteriorate about	...	*
Objective 5	defq	is allowed to deteriorate about	... 0.8	ok !

Taking the compromise-solution:

Objective 1	gdp-%	3.60925
Objective 2	ur	4.84580
Objective 3	pc-%	3.22263
Objective 4	L.Bil.	1.62991
Objective 5	defq	3.00812

Would you accept a deterioration of one of the objectives
in order to improve at least one other y / n ... y

Objective 1	gdp-%	is allowed to deteriorate about	...	*	
Objective 2	ur	is allowed to deteriorate about	...	*	
Objective 3	pc-%	is allowed to deteriorate about	...	0.3	ok !
Objective 4	L.Bil.	is allowed to deteriorate about	...	8.0	ok !
Objective 5	defq	is allowed to deteriorate about	...	0.8	

If you want to change this, enter a new value ... 0.0 ok !

Taking the compromise-solution:

Objective 1	gdp-%	3.40625
Objective 2	ur	4.62236
Objective 3	pc-%	3.01284
Objective 4	L.Bil.	3.85525
Objective 5	defq	3.00812

Would you accept a deterioration of one of the objectives
in order to improve at least one other y / n ... n

Optimal solution found !

*The optimal set of instrument values providing this
solution is:*

I N S T R U M E N T S

transv	334.30487
oifs	53.00000
ftiv	16.50000
naz	38.00000
flst	14.50000
exrc	12.50000
rsp	2.50000
opas	185.00000
subv	49.67354
fdbss	0.52000
rrr	0.05500

A1.2 Interactive Economic Policy Optimization using IMGP

*** I M G P ***

Optimize Problem -> P
Print Objectives -> 0
Print Instruments -> I
E N D -> *
->p

*The first payoff-matrix is the same as in the previous
example. As a first step the program presents*

Iteration No. 1

		POTENCY-MATRIX for PROPOSAL SOLUTION		
		Ideal solution	Pessimistic sol.	Solution
gdp-%	(max)	4.11616	1.81586	1.81586
ur	(min)	3.91260	5.35070	5.35070
pc-%	(min)	1.59272	3.94114	3.94114
L.Bil.	(min)	0.00000	23.18498	23.18498
defq	(min)	-0.97516	7.24101	7.24101

Do you accept this solution as final ?

Y = yes / N = no / L = Potency-matrix / P = Payoff-matrix /
S = Efficient solution
-> n

At each interactive stage the decisionmaker has access to information about the Potency - matrix, the Payoff - matrix, and an efficient solution.

Do you want to set aspiration levels ?

N = no / Y = yes

-> y

Are there aspiration levels for objective gdp-%?

N = no / Y = yes / L = Potency-matrix / P = Payoff-matrix /

S = Efficient solution

-> y

Aspiration level ... 3.4 ok !

Are there aspiration levels for objective ur? -> n

Are there aspiration levels for objective pc-%? -> n

Are there aspiration levels for objective |L.Bil.|? -> n

Are there aspiration levels for objective defq? -> y

Aspiration level ... 3.5 ok !

Shall gdp-% be improved?

Y = yes / W = yes (weakly) / N = no / P = Payoff-matrix /

L = Potency-matrix / S = Efficient solution

-> y

Shall ur be improved? -> y

Shall pc-% be improved? -> y

Shall |L.Bil.| be improved? -> w

Shall defq be improved? -> y

Iteration No. 2

POTENCY-MATRIX for TRIAL SOLUTION

		Ideal solution	Pessimistic sol.	Solution
gdp-%	(max)	3.40193	3.40000	3.40000
ur	(min)	4.59689	4.59936	4.59936
pc-%	(min)	2.76507	2.76693	2.76693
L.Bil.	(min)	3.67144	17.38873	17.38873
defq	(min)	3.49618	3.50000	3.50000

Are the changes in the Potency-matrix justified ?

Y = yes / N = no / V = New trial sol. / Q = New Payoff-mat. /

L = Previous proposal sol. / P = Previous Payoff-mat. /

S = Efficient solution / J = Jump back

-> y

The trial solution becomes the new proposal solution.

Do you accept this solution as final ?

Y = yes / N = no / L = Potency-matrix / P = Payoff-matrix /

S = Efficient solution / R = Repeat

-> p

Do you want to set aspiration levels ?

N = no / Y = yes

-> n

Shall gdp-% be improved?

Y = yes / W = yes (weakly) / N = no / P = Payoff-matrix /

L = Potency-matrix / S = Efficient solution

-> n

Shall ur be improved? -> w

Shall pc-% be improved? -> y

Shall |L.Bil.| be improved? -> w

Shall defq be improved? -> n

Further interaction leads to

Iteration No. 4

POTENCY-MATRIX for PROPOSAL SOLUTION

		Ideal solution	Pessimistic sol.	Solution
gdp-%	(max)	3.40096	3.40000	3.40000
ur	(min)	4.59702	4.59835	4.59835
pc-%	(min)	2.76507	2.76600	2.76600
L.Bil.	(min)	3.68204	13.95941	13.95941
defq	(min)	3.49809	3.50000	3.50000

Do you accept this solution as final ?

Y = yes / N = no / L = Potency-matrix / P = Payoff-matrix /

S = Efficient solution / R = Repeat

-> y

Optimal Solution found !

EFFICIENT SOLUTION

O B J E C T I V E S

gdp-%	(max)	Value	3.40000
ur	(min)	Value	4.59742
pc-%	(min)	Value	2.76600
L.Bil.	(min)	Value	3.69352
defq	(min)	Value	3.49809

The corresponding efficient solution is inspected

I N S T R U M E N T S

transv	342.61415
oifs	53.00000
ftiv	16.19568
naz	38.00000
flst	16.00000
exrc	12.50000
rsp	2.50000
opas	185.00000
subv	50.00000
fdbss	0.52000
rrr	0.05500

A1.3 Interactive Economic Policy Optimization using ZW

*** Z W ***

Optimize Problem -> P

Print Instruments -> I

Print Weights -> W

->p

Choose a set of starting weights y / n ... n

O B J E C T I V E S

gdp-%	(max)	Value	3.76251
ur	(min)	Value	5.01999
pc-%	(min)	Value	3.43331
L.Bil.	(min)	Value	0.00000
defq	(min)	Value	2.90840

The first solution is proposed by assuming equal weights in the objective function. The decision maker could have stated his preferred weighting pattern.

Would you accept
a change of 0.00267 in gdp-% (3.76251) and
a change of -0.04872 in ur (5.01999) and
a change of 0.00720 in pc-% (3.43331) and
a change of 0.00000 in |L.Bil.| (0.00000) and
a change of -0.05991 in defq (2.90840)
---> y / n / ? ... y

Would you accept
a change of -0.00429 in gdp-% (3.76251) and
a change of -0.01040 in ur (5.01999) and
a change of -0.05465 in pc-% (3.43331) and
a change of 0.00000 in |L.Bil.| (0.00000) and
a change of 0.09758 in defq (2.90840)
---> y / n / ? ... ?

Would you accept
a change of 0.01909 in gdp-% (3.76251) and
a change of 0.07858 in ur (5.01999) and
a change of 0.05203 in pc-% (3.43331) and
a change of 0.00000 in |L.Bil.| (0.00000) and
a change of -0.02586 in defq (2.90840)
---> y / n / ? ... n

O B J E C T I V E S
gdp-% (max) Value 3.71965
ur (min) Value 4.91552
pc-% (min) Value 2.88665
|L.Bil.| (min) Value 0.00000
defq (min) Value 3.88745

The decisions result in these values

Would you accept
a change of 0.05900 in gdp-% (3.71965) and
a change of 0.11322 in ur (4.91552) and
a change of 0.73823 in pc-% (2.88665) and
a change of 0.00000 in |L.Bil.| (0.00000) and
a change of -1.39912 in defq (3.88745)
---> y / n / ? ... ?

Would you accept
a change of -0.00429 in gdp-% (3.71965) and
a change of -0.01040 in ur (4.91552) and
a change of -0.05465 in pc-% (2.88665) and
a change of 0.00000 in |L.Bil.| (0.00000) and
a change of 0.09758 in defq (3.88745)
---> y / n / ? ... ?

O B J E C T I V E S
gdp-% (max) Value 3.71965
ur (min) Value 4.91552
pc-% (min) Value 2.88665
|L.Bil.| (min) Value 0.00000
defq (min) Value 3.88745

Optimal solution found !

*** Z W ***
Optimize Problem -> P
Print Instruments -> I
Print Weights -> W
->i

I N S T R U M E N T S
transv 345.65067
oifs 53.00000
ftiv 16.50000
naz 38.00000
flst 14.50000
exrc 12.50000
rsp 2.50000
opas 185.00000
subv 50.00000
fdbss 0.52000
rrr 0.05500

*** Z W ***
Optimize Problem -> P
Print Instruments -> I
Print Weights -> W
->w

W E I G H T S
gdp-% 0.52822
ur 0.40484
pc-% 0.02231
|L.Bil.| 0.02231
defq 0.02231

A1.4 Screen of the Interaction Phase in DIDAS

IAC - DIDAS - L2 V 5.4 Interaction		Names		flst	exrc	rsp	opas	subv
		Upper bound		16.	12.5	4.	185.	50.
		Value		16.	12.5	2.5	185.	50.
		Lower bound		14.5	12.5	2.5	170.	40.
D89D	1	1	Neutral solution					
Names	Status	Lower bound	Utopia	Value	Reference point	Nadir	Upper bound	Automatic scale
GDP	Max	...	4.12	3.03	3.03	1.82	...	2.3
UR	Min	...	3.91	4.24	4.24	5.35	...	1.44
PC	Min	...	1.59	2.7	2.7	3.94	...	2.35
HDLBx		0.		3.1e-15	...		0.	...
DEFQ	Min	-1.000e7	-0.98	2.9	2.9	7.24	1.000e5	8.22
LBx		0.		-4.4e-15	...		0.	...
abs(LB)	Min	...	0.	8.03	8.03	23.19	...	23.19

F1 - Help

F9 - Exit

IAC - DIDAS - L2 V 5.4 Interaction		Names		flst	exrc	rsp	opas	subv
		Upper bound		16.	12.5	4.	185.	50.
		Value		14.5	12.5	2.5	185.	50.
		Lower bound		14.5	12.5	2.5	170.	40.
D89D	1	2	Example after two attempts					
Names	Status	Lower bound	Utopia	Value	Reference point	Nadir	Upper bound	Automatic scale
GDP	Max	...	4.12	3.4	3.5	1.82	...	0.62
UR	Min	...	3.91	4.59	4.5	5.35	...	0.59
PC	Min	...	1.59	2.7	2.7	3.94	...	1.11
HDLBx		0.		3.1e-15	...		0.	...
DEFQ	Min	-1.000e7	-0.98	3.63	3.	7.24	1.000e5	3.98
LBx		0.		-8.8e-15	...		0.	...
abs(LB)	Min	...	0.	3.62	4.	23.19	...	4.02

F1 - Help

F9 - Exit

APPENDIX B

FIGURE 1

Dynamic effects of an increase in public transfers to private households

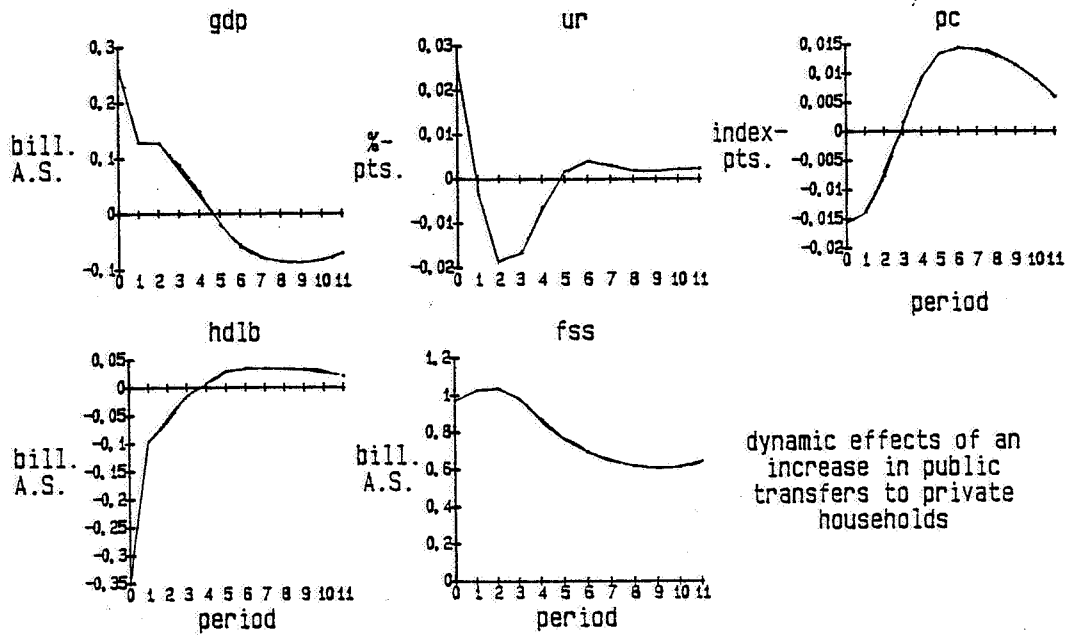


FIGURE 2

Dynamic effects of an increase in public investment expenditures

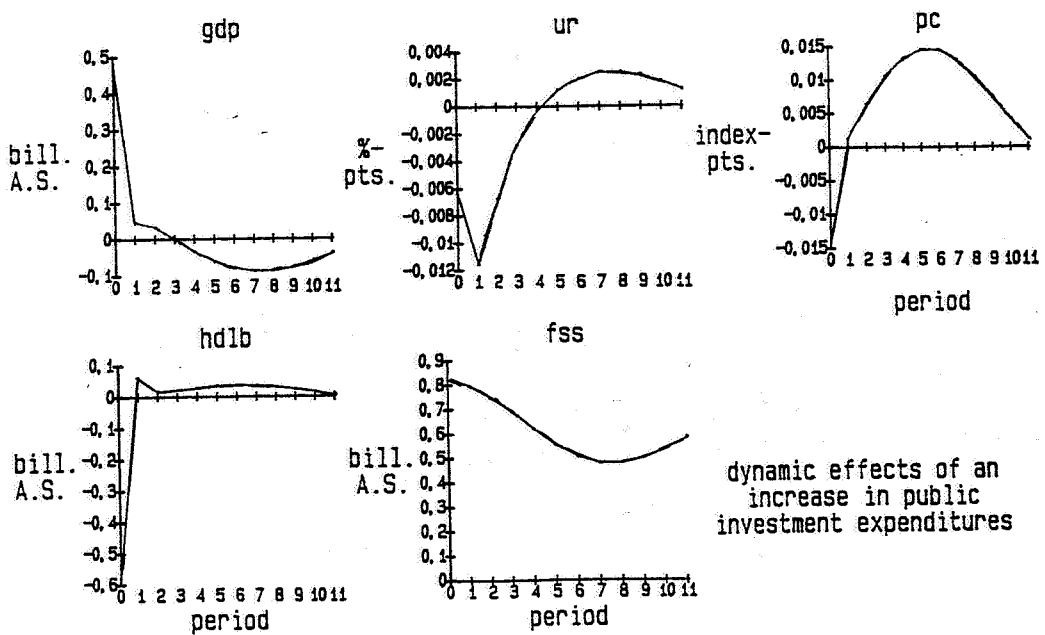
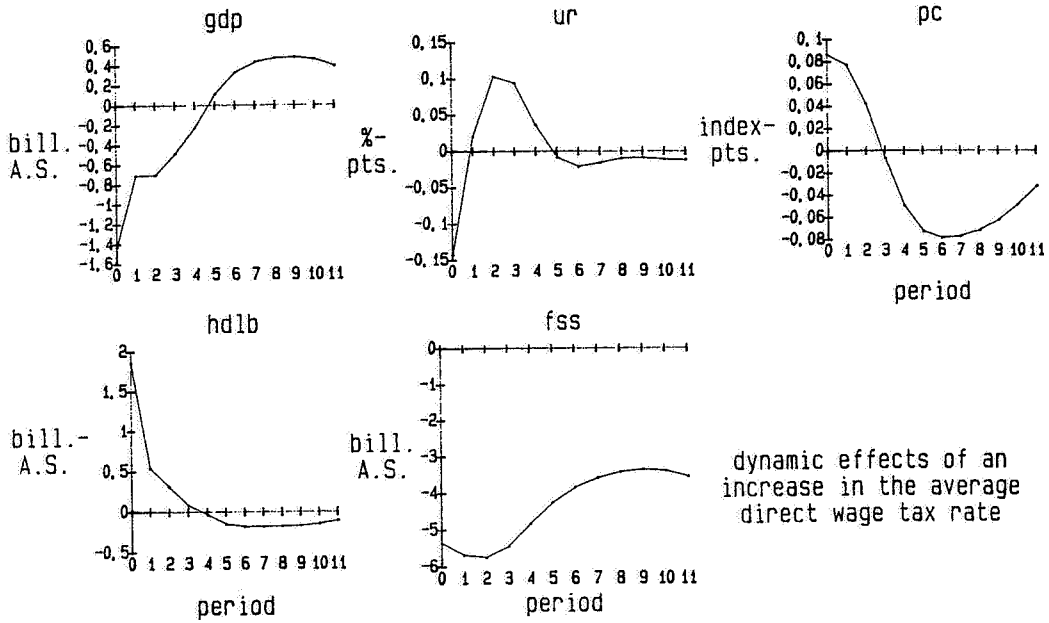


FIGURE 3

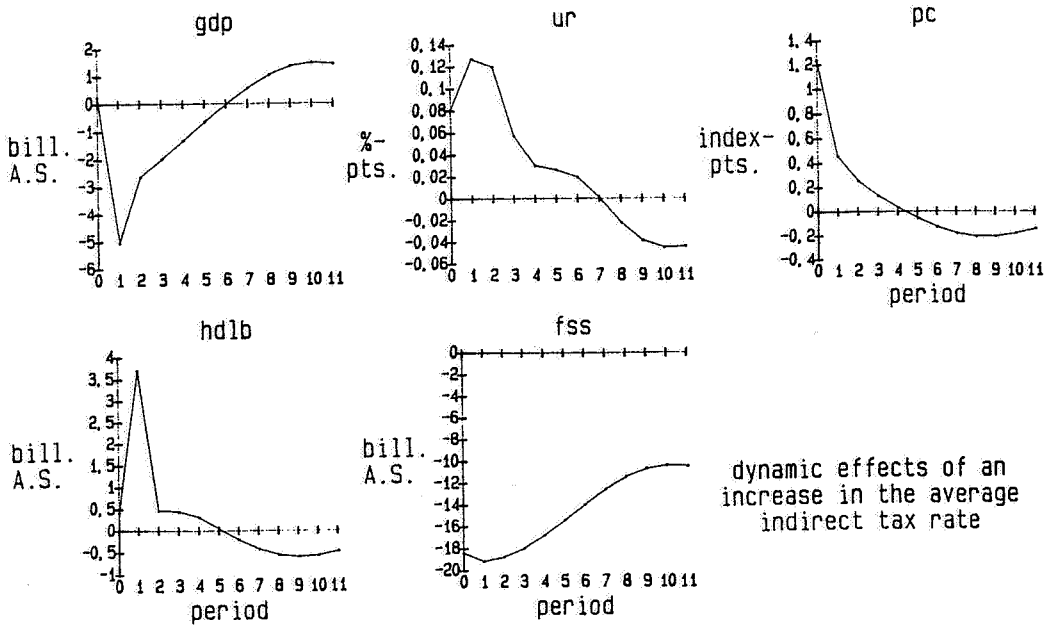
Dynamic effects of an increase in the average direct wage tax rate



dynamic effects of an increase in the average direct wage tax rate

FIGURE 4

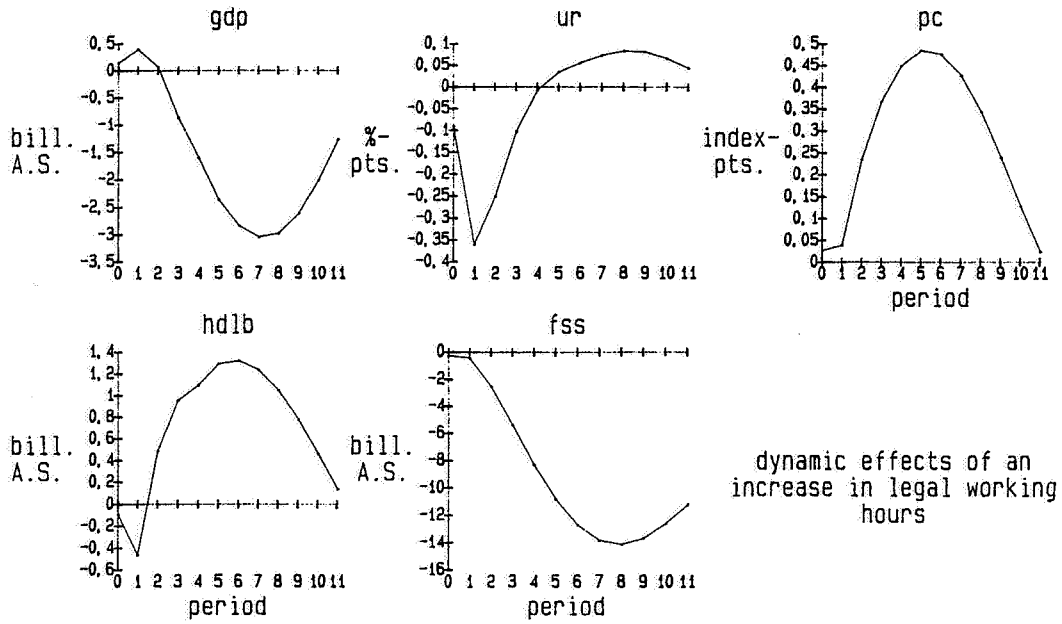
Dynamic effects of an increase in the average indirect tax rate



dynamic effects of an increase in the average indirect tax rate

FIGURE 5

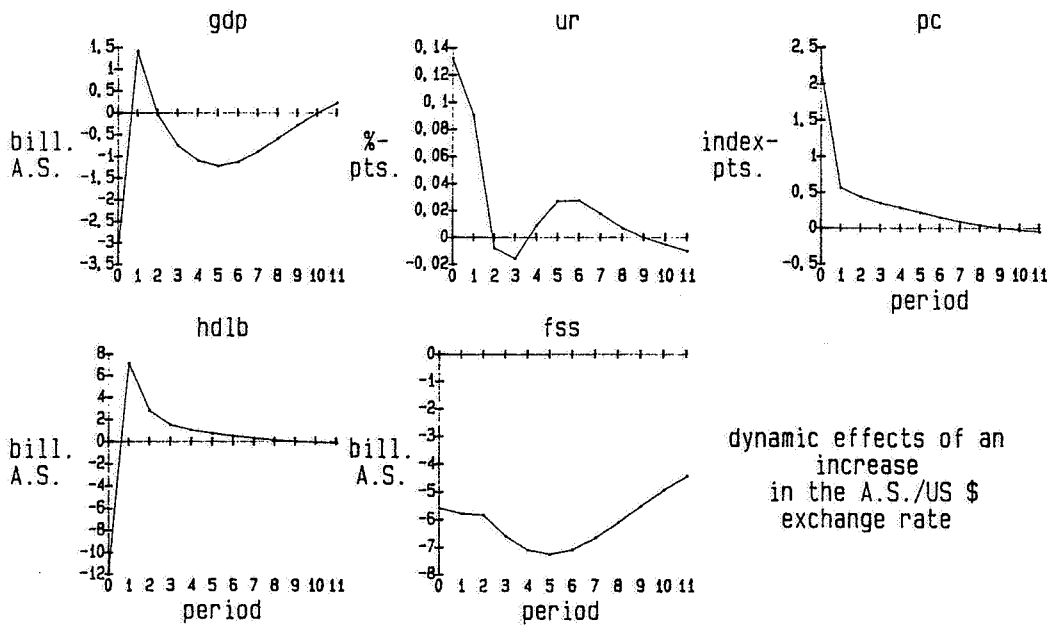
Dynamic effects of an increase in legal working hours



dynamic effects of an increase in legal working hours

FIGURE 6

Dynamic effects of an increase in the A.S./US\$ exchange rate



dynamic effects of an increase in the A.S./US \$ exchange rate

FIGURE 7

Dynamic effects of an increase in the interest rate on savings deposits

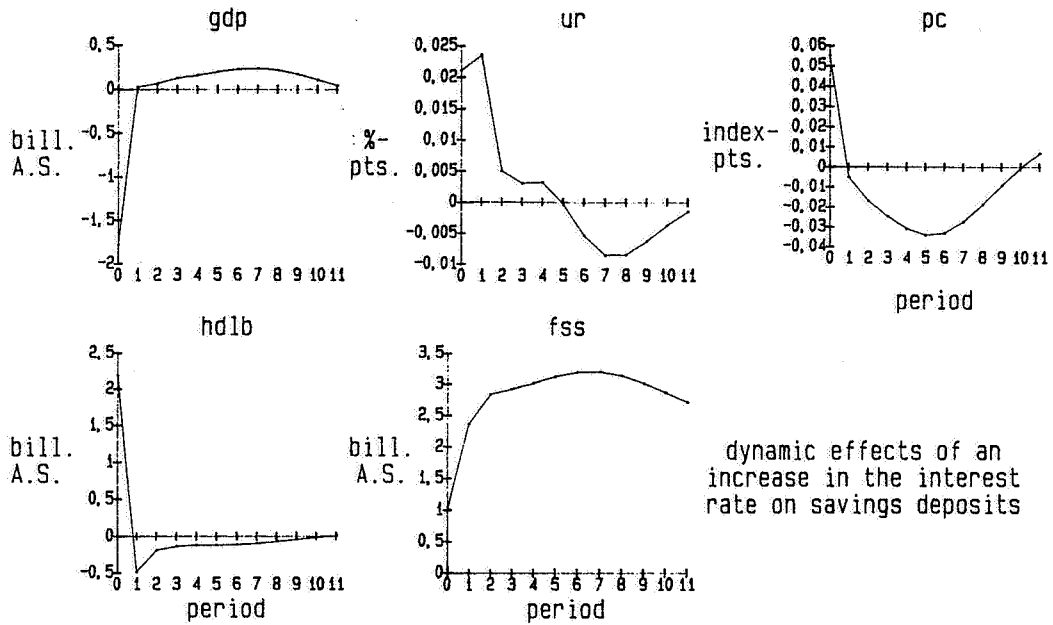


FIGURE 8

Dynamic effects of an increase in salaries of civil servants

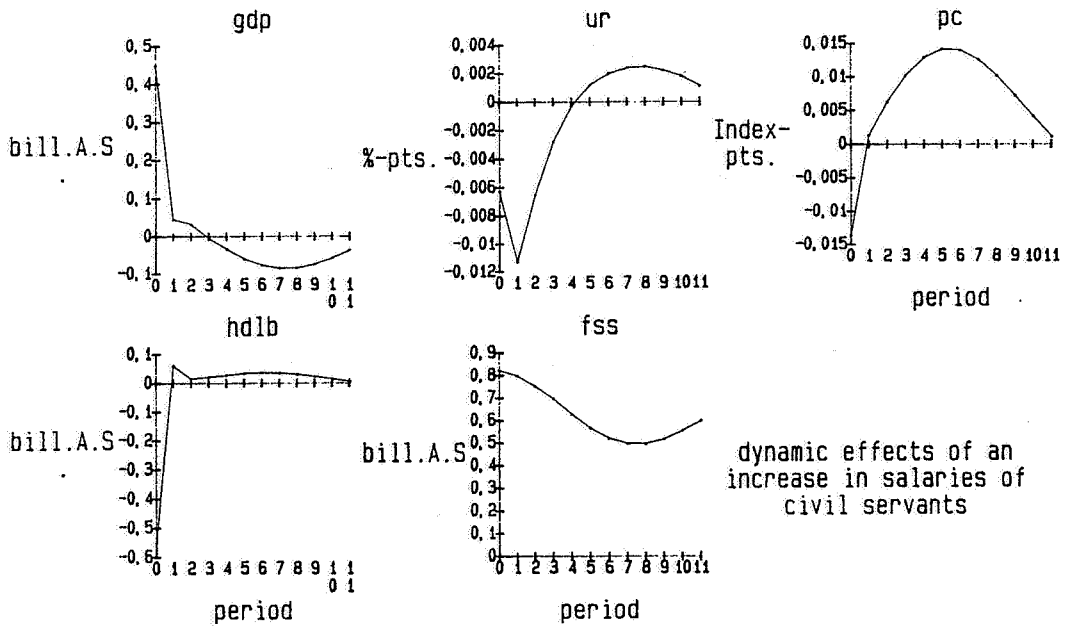


FIGURE 9

Dynamic effects of an increase in subsidies

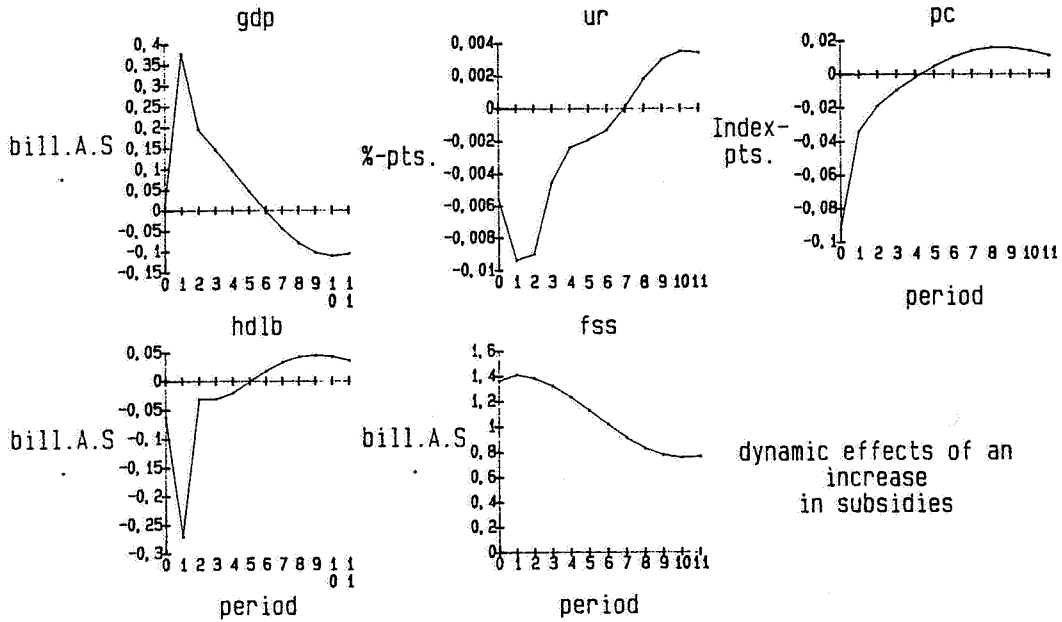


FIGURE 10

Dynamic effects of an increase in the share of employers contributions to social security

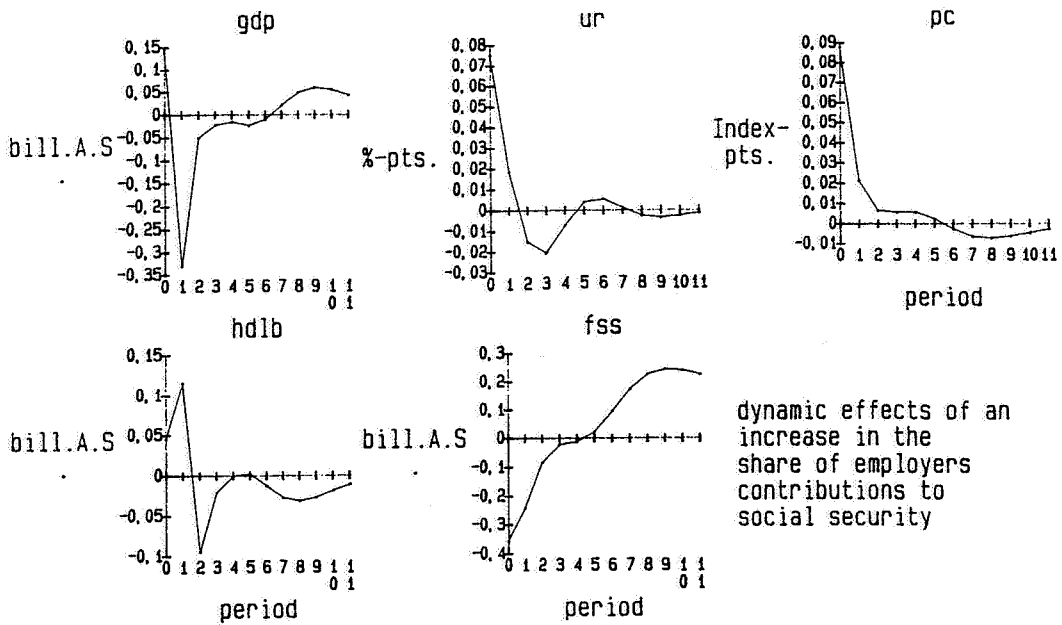
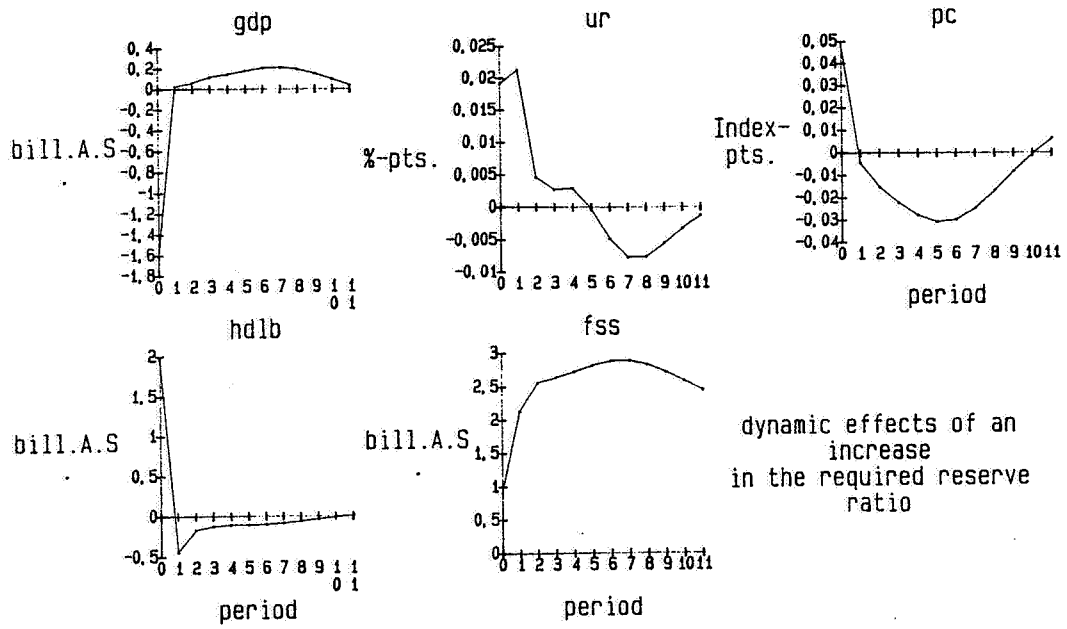


FIGURE 11

Dynamic effects of an increase in the required reserve ratio



APPENDIX C

Model MAXOPT (E)

Version 7/87

A. ENDOGENEOUS VARIABLES¹⁾

ALVB	contributions to unemployment insurance
BIFP	present value of private tax-depreciations allowances
C	private consumption expenditures, at 1976 prices
CP	public consumption expenditures, at 1976 prices
CPS	public consumption expenditures, at current prices
CS	private consumption expenditures, at current prices
DBSS	employers contributions to social insurance
DEF	net deficit/surplus of public sector
DEFQ	deficit ratio
DEPS	depreciations (nat. acc.), at current prices
EBU	total income from profits and property
EBUS	residual income from profits and property
EBUST	government income from profits and property
EGK	retained profits from corporate enterprises
FITS	mark-up factor for indirect taxation minus subsidies
FSS	stock of public sector debt
GDP	Gross domestic product at 1976 market prices
GDPS	Gross domestic product, at current prices
HBU	average weekly working time
HDLB	XS - MS (balance of trade and services)
IF0	gross fixed investment, at 1976 prices
IFP	private gross fixed investment, at 1976 prices
IFS	gross fixed investment, at current prices
KP	private stock of fixed capital, at 1976 prices
LE0	employment
LF	labour supply
LST	direct taxes on wage income
M	imports of goods and services, at 1976 prices
M3	money stock (currency, demand- and savings deposits)
MS	imports of goods and services, at current prices
MU3	money multiplier for M3
OESP	public savings (nat. acc.)
PC	deflator of private consumption
PCP	deflator of public consumption
PDEP	deflator of depreciations (nat. acc.)
PGDP	deflator of gross domestic product
PIF	deflator of gross fixed investment
PM	deflator of imports of goods and services
PMS	deflator of imports of goods and services (in US-\$)
PVD	deflator of domestic demand
PVDN	deflator of domestic demand, (netto ind.St-Subv.)
PX	deflator of exports of goods and services
PXST	deflator of tourism exports
RPI	rental price of private capital
RSECL	effective interest rate on newly issued bonds
RTG	call money rate
SVB	contributions to social insurance
TDHV	direct taxes of private households (nat. acc.)
TDHVR	other direct taxes of private households
TDKV	direct taxes of corporations
TIV	indirect taxes (nat. acc.)
TRANSH	transferincome, gross
ULC	unit labour costs
UR	unemployment rate
VDS	domestic demand, at current prices
WBFB	contributions to construction programs
XS	exports of goods and services, at current prices
XSTS	tourism exports, at current prices

1) Note: Quantities are measured in billions of Austrian Shillings, all prices are 100 in 1976.

XX	exports of goods and services, at 1976 prices
YDS	disposable income, at current prices
YDSG	disposable nonwage income, at current prices
YDSW	disposable wage income, at current prices
YG	disposable nonwage income, at 1976 prices
YS	national income at factor costs, at current prices
YW	disposable wage income, at 1976 prices
YWGGLE	gross wage rate (incl. social wage)
YWGGS	gross wages and salaries (incl. social wage)
YWGH	hourly wage rate
YWGS	gross wages and salaries (excl. social wage)
ZG	base money
ZKSV	interest on consumer debt
ZSSV	interest on public debt

B. EXOGENEOUS VARIABLES

D7390	Dummy 1973 - 1990
D77	Dummy 1977
D78	Dummy 1978
D8384	Dummy 1983:1.0, 1984:-1.0
DD	normal depreciation rate
DDV	advanced depreciation rate
DEFR	difference between changes in public debt and deficit of all public households
DIFII	inventory changes and statistical discrepancy, at 1976 prices
DP	average depreciation rate (nat. acc.)
EWBC	population in working age
EXRC	exchange rate AS/US\$
FDBSS	average rate for employers contributions to social insurance
FIFMS	share of value added tax for public investment
FIMP	share of imputed pensions of public sector
FLST	average wage tax rate
FODEP	share of depreciations of the public sector
FOTIV	share of indirect taxes of public sector
FTIV	average indirect tax rate
FXST	share of tourism exports of total exports of goods and services, at 1976 prices
GDPOECD	gross domestic product of OECD-countries, at 1976 prices
GUS	public fees and penalties
IFMS	value added tax of not-exempted investors
IMPPS	imputed contributions to public pensions
NAZ	legal working time
NP	years of normal depreciation
OIFS	public investment expenditures, at current prices
OIMVS	intermediary consumption of public sector
OKES	refunds for certain public sector costs
OKTRN	capital transfers of public sector, net
OLIEGN	public acquisition of land, net
OPAS	expenditures on civil servants
OTRAN	current transfer receipts of public sector, net
PGDPOECD	deflator of gross domestic product of total OECD
PHHV	contributions to federal government pensions
RDISK	discount rate
REU3	3-month eurodollar rate
RRR	effective required reserve ratio
RSP	basic interest rate on savings deposits
RTGDM	call money rate, FR Germany
SUBV	subsidies (nat. acc.)
T1	time trend
TRANSV	domestic transfer income of private households
U	marginal corporate tax rate
YDREST	net foreign transfers of private households
YFS	factor income from abroad, net

C. RESIDUALS

PCR difference between observed and estimated consumer
 price inflation
 R2 (transh-equation)
 R8 (c-equation)
 R10 (kp-equation)
 R13 (m-equation)
 R14 (xx-equation)
 R16 (rtg-equation)
 R18 (rsecl-equation)
 R20 (hbu-equation)
 R21 (le0-equation)
 R22 (lf-equation)
 R24 (svb-equation)
 R25 (alvb-equation)
 R26 (wfb-equation)
 R35 (pvdn-equation)
 R38 (ywh-equation)
 R40 (pif-equation)
 R42 (pdep-equation)
 R43 (pcp-equation)
 R44 (px-equation)
 R45 (pxst-equation)
 R59 (zksv-equation)
 R60 (zssv-equation)
 R62 (egk-equation)
 R63 (ebust-equation)
 R65 (tdkv-equation)
 R67 (tdhvr-equation)
 RMU3 (mu3-equation)
 RN4 (yds-w-equation)
 RPMS (pms-equation)
 RZG (zg-equation)

D. EQUATION SYSTEM OF THE MACRO MODEL MAXOPT (E) VERSION 7/87

EQUATION 1: YDS DISPOSABLE INCOME, AT CURRENT PRICES

$$\begin{aligned}
 \text{YDS} = & \text{YWGS} + \text{EBUS} - \text{ZKSV} + \text{TRANSV} \\
 & - \text{TDHV} - \text{SVB} - \text{IMPPS} - \text{GUS} - \text{YDREST}
 \end{aligned}$$

EQUATION 2: TRANSH TRANSFER INCOME, GROSS

$$\begin{aligned}
 \text{TRANSH} = & \text{EXP}(\text{LN}(\text{TRANSH1}) + .9913 * \text{LN}(\text{TRANSV}/\text{TRANSV1}) + \\
 & \quad \quad \quad (.00313) \\
 & \quad .25607 * \text{LN}(\text{TRANSV1}) - .25697 * \text{LN}(\text{TRANSH1}) + .00881 + \text{R2} \\
 & \quad (.19399) \quad \quad \quad (.19465) \quad \quad \quad (.00608) \\
 \text{R2} = & .999 \quad \text{DW} = 1.699 \quad \text{SE} = .0003 \quad (1965-84)
 \end{aligned}$$

EQUATION 3: CPS PUBLIC CONSUMPTION, AT CURRENT PRICES

$$\begin{aligned}
 \text{CPS} = & \text{OPAS} + (\text{FIMP} * \text{IMPPS}) + (\text{FODEP} * \text{DEPS}) + (\text{FOTIV} * \text{TIV}/100) \\
 & + \text{OIMVS} - \text{OKES}
 \end{aligned}$$

EQUATION 4: YDSW DISPOSABLE WAGE INCOME, CURRENT PRICES

$$\begin{aligned}
 \text{YDSW} = & \text{YWGS} + \text{TRANSH} - \text{LST} - \text{PHHV} \\
 & - (1 - \text{FDBSS}) * (\text{SVB} - \text{PHHV} + \text{ALVB} + \text{WBFB}) + \text{RN4}
 \end{aligned}$$

EQUATION 5: YDSG DISPOSABLE NONWAGE INCOME, CURR. PRICES

$$\text{YDSG} = \text{YDS} - \text{YDSW}$$

EQUATION 6: YW DISPOSABLE WAGE INCOME, AT 1976 PRICES

YW = YDSW/PC*100

EQUATION 7: YG DISPOSABLE NONWAGE INCOME, 1976 PRICES

YG = YDSG/PC*100

EQUATION 8: C PRIVATE CONSUMPTION, AT 1976 PRICES

C = EXP(LN(C1) + .51688*(LN(YW/YW1)) + .05658*(LN(YG/YG1)) +
(.09356) (.02080)
.32815*(LN(YW1)) + .07954*(LN(YG1)) - .41685*LN(C1) +
(.12005) (.02372) (.15021)
.02705*(D77-D78) + .01707*(D8384) + .22928 + R8)
(.00565) (.00574) (.13536)
R2=.928 DW=1.668 SE=.0074 (1965-84)

EQUATION 9: CP PUBLIC CONSUMPTION, AT 1976 PRICES

CP = CPS*100/PCP

EQUATION 10: KP PRIVATE STOCK OF CAPITAL, AT 1976 PRICES

KP= EXP(LN(KP1) + .09117*LN(GDP/GDP1) + .03808*LN(GDP1/KP1) -
(.03898) (.00925)
.00741*LN(RPI/PGDP) + .05179 + R10)
(.00192) (.01347)
R2=.990 DW=1.010 SE=.0027 (1965-84)
AR1(F1,15)=3.22 ARCH (F1,14)=15.57

EQUATION 11: IFP PRIVATE GROSS FIXED INVESTMENT,
AT 1976 PRICES

IFP = KP - (1-DP)*KP1 + IFMS*(1-FIFMS)

EQUATION 12: IF0 GROSS FIXED INVESTMENT, AT 1976 PRICES

IF0= IFP + OIFS/PIF*100

EQUATION 13: M IMPORTS OF GOODS AND SERVICES,
AT 1976 PRICES

M = EXP(LN(M1) + 2.02832*LN(GDP/GDP1) + 1.06213*LN(GDP1/M1)
(.38382) (.35554)
-.43756*(LN(PM1/(PGDP1*M1)) - 3.56724 + R13)
(.14389) (1.17220)
R2=.837 DW=1.46 SE=.0249 (1965-84)

EQUATION 14: XX EXPORTS OF GOODS AND SERVICES,
AT 1976 PRICES

XX = EXP(LN(XX1) + .67772*LN(GDPOECD/GDPOECD1)
(.44650)
+ 1.93926*LN(GDPOECD1) + .13664*LN(PGDPOECD*EXRC) -
(.44662) (.09866)
.38542*LN(PX) - .73986*LN(XX1) - 12.21234 + R14)
(.20802) (.19911) (2.92150)
R2=.706 DW=2.41 SE=.0289 (1966-84)

EQUATION 15: GDP GROSS DOMESTIC PRODUCT, AT 1976 PRICES

GDP = C + CP + IF0 + XX + DIFII - M

EQUATION 16: RTG CALL MONEY RATE

$$\begin{aligned} \text{RTG} = & \text{EXP}(\text{LN}(\text{RTG1}) + .17764 * \text{LN}(\text{RTGDM}) - .21369 * \text{LN}(\text{RTGDM1}) \\ & \quad (.11022) \quad (.11366) \\ & + .97618 * \text{LN}(\text{RDISK}) - .57498 * \text{LN}(\text{RDISK1}) \\ & \quad (.22200) \quad (.25491) \\ & - .31992 * \text{LN}(\text{RTG1}) + \text{R16} \\ & \quad (.20905) \\ & \text{R2} = .767 \quad \text{DW} = 1.810 \quad \text{SE} = .1451 \quad (1965-84) \end{aligned}$$

EQUATION 17: MU3 MONEY MULTIPLIER FOR M3

$$\begin{aligned} \text{MU3} = & \text{EXP}(.36428 * \text{LN}(\text{GDPS}) - .23449 * \text{LN}(\text{RRR}) - .17808 * \text{LN}(\text{RSP}) \\ & \quad (.01718) \quad (.05655) \quad (.04587) \\ & - 1.23761 + \text{RMU3} \\ & \quad (.07945) \\ & \text{R2} = .993 \quad \text{DW} = 1.66 \quad \text{SE} = .0207 \quad (1964-84) \end{aligned}$$

EQUATION 18: ZG BASE MONEY

$$\begin{aligned} \text{ZG} = & \text{EXP}(\text{LN}(\text{ZG1}) + .62897 * (\text{LN}(\text{XS}) - \text{LN}(\text{MS})) + .10885 * \text{LN}(\text{RTG}/\text{REU3}) \\ & \quad (.27757) \quad (.04132) \\ & + .11143 + \text{RZG} \\ & \quad (.04132) \\ & \text{R2} = .317 \quad \text{DW} = 1.88 \quad \text{SE} = .0358 \quad (1965-84) \end{aligned}$$

EQUATION 19: M3 MONEY STOCK M3

$$\text{M3} = \text{MU3} * \text{ZG}$$

EQUATION 20: RSECL YIELD OF NEWLY ISSUED BONDS

$$\begin{aligned} \text{RSECL} = & \text{EXP}(\text{LN}(\text{RSECL1}) + .14863 * \text{LN}(\text{RTG}/\text{RTG1}) + .16419 * \text{LN}(\text{RTG1}) \\ & \quad (.04013) \quad (.04833) \\ & - .14431 * \text{LN}(\text{RSECL1}) - 1.96900 * \text{LN}((\text{M3}/\text{PC})/(\text{M31}/\text{PC1})) \\ & \quad (.11624) \quad (.34633) \\ & - .16873 * \text{LN}(\text{M31}/\text{PC1}) + .34969 + \text{R18} \\ & \quad (.04534) \quad (.17632) \\ & \text{R2} = .910 \quad \text{DW} = 2.130 \quad \text{SE} = .0307 \quad (1966-84) \end{aligned}$$

EQUATION 21: BIFP PRESENT VALUE OF PRIVATE DEPRECIATIONS OF TAX ALLOWANCES

$$\begin{aligned} \text{BIFP} = & ((1/(1+\text{RSECL}/100))^{.5}) * (\text{DDV} + \text{DD} * (1/(1+\text{RSECL}/100))) \\ & * ((1/(1+\text{RSECL}/100))^{NP-1}) / ((1/(1+\text{RSECL}/100))^{-1}) + \\ & (1 - \text{DDV} - \text{DD} - \text{NP} * \text{DD}) * ((1/(1+\text{RSECL}/100))^{(NP+1)}) \end{aligned}$$

EQUATION 22: HBU AVERAGE WEEKLY WORKING TIME

$$\begin{aligned} \text{HBU} = & \text{EXP}(\text{LN}(\text{HBU1}) + .54748 * \text{LN}(\text{NAZ}/\text{NAZ1}) + .49318 * \text{LN}(\text{NAZ1}) \\ & \quad (.08225) \quad (.12096) \\ & + .13041 * \text{LN}(\text{GDP}/\text{GDP1}) - .53745 * \text{LN}(\text{HBU1}) + .12282 + \text{R20} \\ & \quad (.07162) \quad (.12502) \quad (.10195) \\ & \text{R2} = .830 \quad \text{DW} = 1.848 \quad \text{SE} = .0052 \quad (1965-84) \end{aligned}$$

EQUATION 23: LEO EMPLOYMENT

$$\begin{aligned} \text{LEO} = & \text{EXP}(\text{LN}(\text{LE1}) + .19798 * \text{LN}((\text{GDP}/\text{GDP1})/(\text{HBU}/\text{HBU1})) \\ & \quad (.09213) \\ & + .38355 * \text{LN}(\text{GDP1}/(\text{HBU1} * \text{LE1})) - .12239 * \text{LN}((\text{YWGGLE}/(\text{HBU} * \text{PGDP}))) \\ & \quad (.07347) \quad (.04937) \\ & - .00794 * \text{T1} + 1.61687 + \text{R21} \\ & \quad (.00168) \quad (.48672) \\ & \text{R2} = .849 \quad \text{DW} = 1.43 \quad \text{SE} = .0067 \quad (1965-84) \end{aligned}$$

EQUATION 24: LF LABOUR SUPPLY

$$LF = \text{EXP}(\text{LN}(\text{EWBC}) + \text{LN}(\text{LF1}/\text{EWBC1}) - .05448 * (\text{LN}(\text{LF1}/\text{EWBC1})))$$

$$\begin{array}{r}
 (.17275) \\
 -.52453 * (\text{LN}(\text{LF2}/\text{EWBC2})) + .24205 * \text{LN}(\text{YW}/\text{YW1}) + .10481 * \text{LN}(\text{YW1}) \\
 (.13131) \quad (.05999) \quad (.02216) \\
 -.02766 * \text{LN}(\text{YG}/\text{YG1}) - .02445 * \text{LN}(\text{YG1}) - .81652 + \text{R22} \\
 (.01128) \quad (.01247) \quad (.15593) \\
 \text{R2} = .898 \quad \text{DW} = 2.04 \quad \text{SE} = .0039 \quad (1966-84)
 \end{array}$$

EQUATION 25: UR UNEMPLOYMENT RATE

$$UR = (\text{LF} - \text{LE0}) / \text{LF} * 100.$$

EQUATION 26: SVB CONTRIBUTIONS TO SOCIAL INSURANCE

$$SVB = \text{EXP}(\text{LN}(\text{SVB1}) + .6447 * (\text{LN}(\text{YWGS}/\text{YWGS1})) + .29959 * \text{LN}(\text{YWGS1}))$$

$$\begin{array}{r}
 (.12295) \quad (.10563) \\
 -.26257 * \text{LN}(\text{SVB1}) + .06652 * \text{D78} - .54019 + \text{R24} \\
 (.09041) \quad (.01588) \quad (.21192) \\
 \text{R2} = .891 \quad \text{DW} = 1.602 \quad \text{SE} = .0143 \quad (1965-84)
 \end{array}$$

EQUATION 27: ALVB CONTRIBUTIONS TO UNEMPLOYMENT INSURANCE

$$ALVB = \text{EXP}(\text{LN}(\text{YWGS}) + \text{LN}(\text{ALVB1}/\text{YWGS1}) + .26745 * \text{LN}(\text{UR}/\text{UR1}))$$

$$\begin{array}{r}
 (.06236) \\
 + .01486 * \text{T1} + .24511 * \text{LN}(\text{UR1} * \text{YWGS1} / \text{ALVB1}) - 1.40207 + \text{R25} \\
 (.00233) \quad (.06559) \quad (.35732) \\
 \text{R2} = .853 \quad \text{DW} = 2.839 \quad \text{SE} = .0382 \quad (1966-84)
 \end{array}$$

EQUATION 28: WFBF CONTRIBUTIONS TO CONSTRUCTION PROGRAMS

$$WFBF = \text{EXP}(\text{LN}(\text{WFBF1}) + .4837 * (\text{LN}(\text{YWGS}/\text{YWGS1})) + .50138 * \text{LN}(\text{YWGS1}))$$

$$\begin{array}{r}
 (.24517) \quad (.14798) \\
 -.45521 * \text{LN}(\text{WFBF1}) - 2.52922 + \text{R26} \\
 (.13989) \quad (.74849) \\
 \text{R2} = .666 \quad \text{DW} = 2.449 \quad \text{SE} = .0284 \quad (1965-84)
 \end{array}$$

EQUATION 29: DBSS EMPLOYERS CONTRIBUTIONS TO SOCIAL INSUR.

$$DBSS = \text{FDBSS} * (\text{ALVB} + \text{WFBF} + \text{SVB} - \text{PHHV})$$

EQUATION 30: YWGS GROSS WAGES AND SALARIES (INCL. SOCIAL WAGE)

$$YWGS = \text{YWGS} + \text{IMPPS} + \text{DBSS}$$

EQUATION 31: ULC UNIT LABOUR COSTS(YWGS/GDP)

$$ULC = \text{YWGS} / \text{GDP}$$

EQUATION 32: YWGGLE GROSS WAGE RATE (INCL. SOCIAL WAGE)

$$YWGGLE = \text{YWGS} / \text{LE0} * 1000$$

EQUATION 33: TIV INDIRECT TAXES (NAT. ACC.)

$$\text{TIV} = (\text{FTIV} / 100) * (\text{CS} + \text{CPS} + \text{XSTS} + \text{IFS})$$

EQUATION 34: PMS DEFLATOR IMPORTS OF GOODS AND SERVICES
(BASED ON US\$)

$$PMS = \text{EXP}(\text{LN}(PMS1) + 1.81228 * \text{LN}(PGDPOECD/PGDPOCD1) + (.15481) \\ + .14093 * \text{LN}(PGDPOCD1/PMS1) - .00004 + RPMS) \\ (.07845) \quad (.03038) \\ R2=.890 \quad DW=2.606 \quad SE=.0316 \quad (1965-84)$$

EQUATION 35: PM DEFLATOR IMPORTS OF GOODS AND SERVICES
(BASED ON A.S.)

$$PM = PMS * \text{EXRC} / 17.93925$$

EQUATION 36: FITS MARK-UP FACTOR FOR IND.TAXES & SUBSIDIES

$$\text{FITS} = (\text{TIV} - \text{SUBV}) / (\text{CS} + \text{CPS} + \text{XSTS} + \text{IFS})$$

EQUATION 37: PVDN NET PRICE DEFLATOR OF DOMESTIC DEMAND

$$PVDN = \text{EXP}(\text{LN}(PVDN1) + .34162 * (\text{LN}(ULC/ULC1)) \\ (.07123) \\ + .31499 * (\text{LN}(PM/PM1)) + .13727 * \text{LN}(ULC1/PVDN1) \\ (.06224) \quad (.08399) \\ + .09875 * \text{LN}(PM1/PVDN1) + .73921 + R35) \\ (.07756) \quad (.43919) \\ R2=.982 \quad DW=1.780 \quad SE=.0089 \quad (1965-84)$$

EQUATION 38: PVD DEFLATOR DOMESTIC DEMAND

$$PVD = (1 + \text{FITS}) * PVDN / 1.1262199$$

EQUATION 39: PC DEFLATOR OF PRIVATE CONSUMPTION

$$PC = \text{EXP}(\text{LN}(PC1) + .69868 * (\text{LN}(PVD/PVD1)) + .34734 * (\text{LN}(PVD1/PC1)) \\ (.08862) \quad (.08870) \\ + .01729 + \text{PCR}) \\ (.00536) \\ R2=.896 \quad DW=2.145 \quad SE=.0062 \quad (1965-84)$$

EQUATION 40: YWGH GROSS HOURLY WAGE RATE

$$YWGH = \text{EXP}(\text{LN}(YWGH1) + 1.02478 * (\text{LN}(PC/PC1) - \text{PCR}) + \\ (.28648) \\ + .07763 * \text{LN}(PC1/YWGH1) - .03299 * \text{LN}(UR) + \\ (.01592) \quad (.01346) \\ - .50820 * \text{LN}(NAZ/NAZ1) + .01134 + R38) \\ (.20752) \quad (.03190) \\ R2=.856 \quad DW=2.524 \quad SE=.0131 \quad (1965-84)$$

EQUATION 41: YWGS GROSS WAGES AND SALARIES
(EXCL. SOCIAL WAGE)

$$YWGS = (YWGH * (\text{HBU} * 52) / 1000) * \text{LEO} / 1000$$

EQUATION 42: PIF DEFLATOR OF GROSS FIXED INVESTMENT

$$PIF = \text{EXP}(\text{LN}(PIF1) + .99472 * (\text{LN}(PVD/PVD1)) + .36003 * \text{LN}(PVD1) \\ (.17976) \quad (.18738) \\ - .39277 * \text{LN}(PIF1) + .15537 + R40) \\ (.20451) \quad (.09698) \\ R2=.730 \quad DW=1.491 \quad SE=.0140 \quad (1965-84)$$

EQUATION 43: PDEP DEFLATOR DEPRECIATION (NAT. ACC.)

$$\begin{aligned} \text{PDEP} = & \text{EXP}(\text{LN}(\text{PDEP1}) + .86433 * \text{LN}(\text{PIF}/\text{PIF1}) \\ & \quad (.11962) \\ & + .19831 * \text{LN}(\text{PIF1}/\text{PDEP1}) + .00652 + \text{R42} \\ & \quad (.17337) \quad (.00674) \\ & \text{R2} = .784 \quad \text{DW} = 1.821 \quad \text{SE} = .0110 \quad (1965-84) \end{aligned}$$

EQUATION 44: PCP DEFLATOR PUBLIC CONSUMPTION

$$\begin{aligned} \text{PCP} = & \text{EXP}(\text{LN}(\text{PCP1}) + .94832 * (\text{LN}(\text{YWGGLE}/\text{YWGGLE1})) + \\ & \quad (.13287) \\ & .49227 * \text{LN}(\text{YWGGLE1}) - .57614 * \text{LN}(\text{PCP1}) + .17915 + \text{R43} \\ & \quad (.18932) \quad (.22208) \quad (.08148) \\ & \text{R2} = .809 \quad \text{DW} = 1.841 \quad \text{SE} = .0122 \quad (1965-84) \end{aligned}$$

EQUATION 45: PX DEFLATOR EXPORTS OF GOODS AND SERVICES

$$\begin{aligned} \text{PX} = & \text{EXP}(\text{LN}(\text{PX1}) + .89831 * \text{LN}(\text{PVDN}/\text{PVDN1}) + .54423 * \text{LN}(\text{PVDN1}) \\ & \quad (.13088) \quad (.17316) \\ & - .71578 * \text{LN}(\text{PX1}) + .79371 + \text{R44} \\ & \quad (.22852) \quad (.26030) \\ & \text{R2} = .765 \quad \text{DW} = 1.702 \quad \text{SE} = .0117 \quad (1965-84) \end{aligned}$$

EQUATION 46: PXST DEFLATOR TOURISM EXPORTS

$$\begin{aligned} \text{PXST} = & \text{EXP}(\text{LN}(\text{PXST1}) + 1.11775 * \text{LN}(\text{PC}/\text{PC1}) + .10155 * \text{LN}(\text{PC1}/\text{PXST1}) \\ & \quad (.13613) \quad (.05881) \\ & - .00278 + \text{R45} \\ & \quad (.00808) \\ & \text{R2} = .819 \quad \text{DW} = 2.083 \quad \text{SE} = .0096 \quad (1966-84) \end{aligned}$$

EQUATION 47: CS PRIVATE CONSUMPTION, CURRENT PRICES

$$\text{CS} = \text{PC} * \text{C} / 100$$

EQUATION 48: IFS GROSS FIXED INVESTMENT, CURRENT PRICES

$$\text{IFS} = (\text{IFP} * \text{PIF} / 100) + \text{OIFS}$$

EQUATION 49: VDS DOMESTIC DEMAND, CURRENT PRICES

$$\text{VDS} = (\text{C} + \text{CP} + \text{IF0} + \text{DIF11}) * \text{PVD} / 100$$

EQUATION 50: MS IMPORTS OF GOODS AND SERVICES,
AT CURRENT PRICES

$$\text{MS} = \text{M} * \text{PM} / 100$$

EQUATION 51: XS EXPORTS OF GOODS AND SERVICES,
AT CURRENT PRICES

$$\text{XS} = \text{XX} * \text{PX} / 100$$

EQUATION 52: HDLB TRADE AND SERVICE BALANCE

$$\text{HDLB} = \text{XS} - \text{MS}$$

EQUATION 53: XSTS TOURISM EXPORTS, CURRENT PRICES

$$\text{XSTS} = (\text{FXST} * \text{XX} / 100) * \text{PXST} / 100$$

EQUATION 54: GDPS GROSS DOMESTIC PRODUCT, CURRENT PRICES

$$GDPS = VDS + XS - MS$$

EQUATION 55: PGDP DEFLATOR OF GROSS DOMESTIC PRODUCT

$$PGDP = GDPS/GDP*100$$

EQUATION 56: RPI RENTAL PRICE OF PRIVATE CAPITAL

$$RPI = PIF*(DP+RSECL/100-(PGDP/PGDP1-1))*(1-U*BIFP)/(1-U)$$

EQUATION 57: DEPS DEPRECIATIONS (NAT. ACC.), CURRENT PRICES

$$DEPS = ((DP*KP1)*PDEP/100)/(1-FODEP)$$

EQUATION 58: YS NET NATIONAL PRODUCT AT FACTOR COSTS

$$YS = GDPS - DEPS - TIV + SUBV - YFS$$

EQUATION 59: ZKSV INTEREST ON CONSUMER DEBT

$$\begin{aligned} ZKSV = & \text{EXP}(\text{LN}(ZKSV1)) + .22263*\text{LN}(RSECL/RSECL1) \\ & (.20051) \\ & +1.51081*\text{LN}(CS/CS1) - .03606*\text{LN}(ZKSV1) + .06245 + R59) \\ & (.64625) (.01705) (.06377) \\ & R2=.453 \quad DW=1.622 \quad SE=.0735 \quad (1965-84) \end{aligned}$$

EQUATION 60: ZSSV INTEREST ON PUBLIC DEBT

$$\begin{aligned} ZSSV = & \text{EXP}(\text{LN}(ZSSV1)) + .30797*\text{LN}((RSECL*FSS)/(RSECL1*FSS1)) + \\ & (.09256) \\ & .62858*\text{LN}(RSECL1*FSS1) - .60503*\text{LN}(ZSSV1) - 3.02905 + R60) \\ & (.10153) (.09983) (.50213) \\ & R2=.781 \quad DW=1.667 \quad SE=.0399 \quad (1965-84) \end{aligned}$$

EQUATION 61: EBU TOTAL INCOME FROM PROFITS AND PROPERTY

$$EBU = YS - YWGS + ZSSV + ZKSV$$

EQUATION 62: EGK RETAINED EARNINGS OF CORPORATIONS (NAT. ACC.)

$$\begin{aligned} EGK = & \text{EXP}(\text{LN}(EGK1)) + 5.03564*\text{LN}(GDPS/GDPS1) \\ & (.63089) \\ & + .82678*\text{LN}(GDPS1/EGK1) - 2.68173 + R62) \\ & (.12801) (.38632) \\ & R2=.816 \quad DW=1.505 \quad SE=.0619 \quad (1965-84) \end{aligned}$$

EQUATION 63: EBUST GOVERNMENT INCOME FROM PROFITS AND PROPERTY (NAT. ACC.)

$$\begin{aligned} EBUST = & \text{EXP}(.46932*\text{LN}(RSECL) + .41229*\text{LN}(GDPS) \\ & (.27243) (.19819) \\ & + .63014*\text{LN}(EBUST1) - 2.73539 + R63) \\ & (.13969) (.83770) \\ & R2=.986 \quad DW=1.961 \quad SE=.0921 \quad (1965-84) \end{aligned}$$

EQUATION 64: EBUS RESIDUAL INCOME FROM PROFITS AND PROPERTY

$$EBUS = EBU - EGK - EBUST$$

EQUATION 65: TDKV DIRECT TAXES OF CORPORATIONS

$$\begin{aligned} \text{TDKV} = & \text{EXP}(\text{LN}(\text{TDKV1}) + .45659 * (\text{LN}(\text{EGK1}/\text{EGK2})) + .70434 * \text{LN}(\text{EGK2}) \\ & \quad (.11837) \quad (.15231) \\ & - .63434 * (\text{LN}(\text{TDKV1})) - .17693 * \text{D7390} - .79313 + \text{R65} \\ & \quad (.14615) \quad (.07106) \quad (.22531) \\ & \quad \text{R2} = .655 \quad \text{DW} = 2.047 \quad \text{SE} = .0585 \quad (1966-84) \end{aligned}$$

EQUATION 66: LST DIRECT WAGE TAX

$$\text{LST} = (\text{FLST}/100) * \text{YWGS}$$

EQUATION 67: TDHVR OTHER DIRECT TAXES OF PRIVATE HOUSEHOLDS

$$\begin{aligned} \text{TDHVR} = & \text{EXP}(\text{LN}(\text{TDHVR1}) + 1.65510 * \text{LN}(\text{YWGS}/\text{YWGS1}) \\ & \quad (.28086) \\ & + .19703 * \text{LN}(\text{YWGS1}/\text{TDHVR1}) + .42363 * \text{LN}(\text{EBUS2}/\text{EBUS3}) + \\ & \quad (.08784) \quad (.12596) \\ & + .28171 * \text{LN}(\text{EBUS3}/\text{TDHVR1}) - .87802 + \text{R67} \\ & \quad (.07179) \quad (.26807) \\ & \quad \text{R2} = .835 \quad \text{DW} = 2.812 \quad \text{SE} = .0275 \quad (1967-84) \end{aligned}$$

EQUATION 68: TDHV TOTAL DIRECT TAXES OF PRIVATE HOUSEHOLDS

$$\text{TDHV} = \text{LST} + \text{ALVB} + \text{WBFB} + \text{TDHVR}$$

EQUATION 69: OESP SAVINGS OF THE PUBLIC SECTOR (NAT. ACC.)

$$\text{OESP} = \text{EBUST} + \text{TIV} + \text{TDHV} + \text{TDKV} + \text{SVB} + \text{IMPSS} + \text{GUS} + \text{OTRAN} - \text{CPS} - \text{ZSSV} - \text{SUBV} - \text{TRANSV}$$

EQUATION 70: DEF NET DEFICIT/SURPLUS OF PUBLIC SECTOR

$$\text{DEF} = \text{OESP} + (\text{FODEP} * \text{DEPS}) + \text{OKTRN} - \text{OIFS} - \text{OLIEGN}$$

EQUATION 71: FSS STOCK OF PUBLIC SECTOR DEBT

$$\text{FSS} = \text{FSS1} - \text{DEF} + \text{DEFR}$$

EQUATION 72: DEFQ DEFICIT RATIO

$$\text{DEFQ} = (\text{FSS} - \text{FSS1}) / \text{GDPS} * 100$$

